



THIRD SPACE
LEARNING

GCSE Exam Questions

Quadratic Simultaneous Equations
| Algebra

GCSE Exam Questions: Quadratic Simultaneous Equations

- 1) Solve the simultaneous equations:
- $$xy = 12$$
- $$y - 3x + 9 = 0$$

(5 marks)

- 2) Solve the simultaneous equations:
- $$a^2 + b^2 = 20$$
- $$b + 10 = 2a$$

(5 marks)

- 3) Solve the simultaneous equations:
- $$x^2 - 4y^2 = 9$$
- $$3x + 4y = 7$$

(5 marks)

- 4) Find the distance between
the two points of
intersection of the two lines:
- $$y = 2x^2 - 3x - 10$$
- $$2x - y + 2 = 0$$

(6 marks)

	Question	Answer	Marks
1)	Solve the simultaneous equations $xy = 12$ $y - 3x + 9 = 0$	Rearranging second equation to $y = 3x - 9$ Substitution of $(3x - 9)$ into equation one Correct expansion of bracket, e.g. $3x^2 - 9x = 12$ $3x^2 - 9x - 12 = 0$ Solving for x correctly (4 and -1) Correct substitution of x back into either equations Correct final answer: $x = 4, y = 3$ and $x = -1, y = -12$	(1) (1) (1) (1) (1)
2)	Solve the simultaneous equations $a^2 + b^2 = 20$ $b + 10 = 2a$	Clear attempt for substitution of $2a - 10$ into first equation Correct expansion of at least 3 terms of $(2a - 10)^2$ $4a^2 - 20a - 20a + 100$ oe Simplifying to : $5a^2 - 40a + 80 = 0$ or $a^2 - 8a + 16 = 0$ Correct substitution of a back into either equations for b Correct final answer: $a = 4, b = -2$	(1) (1) (1) (1) (1)

GCSE Exam Questions: Quadratic Simultaneous Equations Answers

	Question	Answer	Marks
3)	Solve the simultaneous equations $x^2 - 4y^2 = 9$ $3x + 4y = 7$	Method to find an expression for y to substitute into first equations E.g $y = \frac{7-3x}{4}$ Correct substitution and expansion E.g. $x^2 - 4(\frac{49 - 42x + 9x^2}{16}) = 9$ Or $4x^2 - 49 + 42x - 9x^2 = 36$ Correct attempt to form a quadratic equation E.g. $5x^2 - 42x + 85 = 0$ Correct method for solving quadratic equations Correct final answer: $x = 3.4, y = -0.8$ $x = 5, y = -2$	(1) (1) (1) (1) (1)
4)	Find the distance between the intersection of the two lines $y = 2x^2 - 3x - 10$ $2x - y + 2 = 0$	Eliminating one unknown E.g $2x + 2 = 2x^2 - 3x - 10$ Correctly rearranging equation to form a quadratic $2x^2 - 5x - 12 = 0$ Correct use of method to solve quadratic for one unknown E.g. completing the square, quadratic formula, or factorisation Use of substitution to find other variable Correct points of intersection seen (-1.5, -1) and (4,10) or $x = -\frac{3}{2}, y = -1$ and $x = 4, y = 10$ Method for distance between two points E.g. Pythagorean Theorem Correct final answer: 12.3 (to 3 sf)	(1) (1) (1) (1) (1) (1)

Where to go next?

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