

Triangular Numbers - Worksheet

Skill

Group A - Finding small triangular numbers using the n th term $\frac{1}{2}n(n + 1)$

Find the following triangular numbers:

- | | | |
|---------|---------|----------|
| 1) 4th | 2) 6th | 3) 16th |
| 4) 12th | 5) 5th | 6) 10th |
| 7) 20th | 8) 1st | 9) 8th |
| 10) 7th | 11) 2nd | 12) 15th |

Group B - Finding big triangular numbers using the n th term $\frac{1}{2}n(n + 1)$

Find the following triangular numbers:

- | | | |
|------------|------------|-------------|
| 1) 50th | 2) 100th | 3) 150th |
| 4) 200th | 5) 202nd | 6) 290th |
| 7) 1000th | 8) 2500th | 9) 2750th |
| 10) 3000th | 11) 6000th | 12) 12000th |

Group C - Identifying triangular numbers

Decide if the numbers below are triangular:

- | | | |
|---------|---------|----------|
| 1) 55 | 2) 77 | 3) 91 |
| 4) 102 | 5) 136 | 6) 210 |
| 7) 351 | 8) 408 | 9) 630 |
| 10) 780 | 11) 821 | 12) 1830 |

Triangular Numbers - Worksheet

Applied

1) Write down the first 10 triangular numbers.

2)

1	12	81	
	39	49	45
	10	78	4

From the box above, identify any triangular numbers.

3) Write down a number less than 100 that is a triangular number and a square number.

4) Which two-digit triangular number with 6 factors is also a multiple of 7?

5) (a) What is the 5th triangular number?

(b) What is the 6th triangular number?

(c) Find the sum of the 5th and 6th triangular number.

(d) What type of number is your answer to part (c)?

6) At a party, everybody shakes hands with each other once.
Work out how many handshakes there are in total, if there are:

(a) 3 people at the party

(b) 7 people at the party

(c) 12 people at the party

Triangular Numbers - Exam Questions

- 1) The pattern below shows the first 4 triangular numbers



- (a) Write down the first four triangular numbers.

.....
(1)

- (b) In the space below, draw pattern 5

.....
(1)

- (c) Write down the 5th triangular number.

.....
(1)
(3 marks)

-
- 2) List the first 6 triangular numbers.

.....
(2 marks)

-
- 3) Find the difference between the 3rd and 6th triangular numbers.

.....
(2 marks)

Triangular Numbers - Exam Questions

- 4) The triangular numbers are 1, 3, 6, 10, ...

The n th term of this sequence is

$$\frac{1}{2}n(n + 1)$$

Find the 250th triangular number.

.....
(2 marks)

- 5) The triangular numbers are 1, 3, 6, 10,...

The n th term of this sequence is

$$\frac{1}{2}n(n + 1)$$

Is 4656 a triangular number?

.....
(3 marks)

Triangular Numbers - Answers

	Question	Answer
	Skill Questions	
Group A	Find the following: 1) 4th triangular number 2) 6th triangular number 3) 16th triangular number 4) 12th triangular number 5) 5th triangular number 6) 10th triangular number 7) 20th triangular number 8) 1st triangular number 9) 8th triangular number 10) 7th triangular number 11) 2nd triangular number 12) 15th triangular number	1) 10 2) 21 3) 136 4) 78 5) 15 6) 55 7) 210 8) 1 9) 36 10) 28 11) 3 12) 120
Group B	Find the following: 1) 50th triangular number 2) 100th triangular number 3) 150th triangular number 4) 200th triangular number 5) 202nd triangular number 6) 290th triangular number 7) 1000th triangular number 8) 2500th triangular number 9) 2750th triangular number 10) 3000th triangular number 11) 6000th triangular number 12) 12 000th triangular number	1) 1 275 2) 5 050 3) 11 325 4) 20 100 5) 20 503 6) 42 195 7) 500 500 8) 3 126 250 9) 3 782 625 10) 4 501 500 11) 18 003 000 12) 72 006 000



Triangular Numbers - Answers

Group C	Decide if the numbers below are triangular: 1) 55 2) 77 3) 91 4) 102 5) 136 6) 210 7) 351 8) 408 9) 630 10) 780 11) 821 12) 1830	1) Yes (10th) 2) No 3) Yes (13th) 4) No 5) Yes (16th) 6) Yes (20th) 7) Yes (26th) 8) No 9) Yes (35th) 10) Yes (39th) 11) No 12) Yes (60th)
----------------	--	---

Triangular Numbers - Answers

	Question	Answer
	Applied Questions	
1)	Write down the first 10 triangular numbers.	1, 3, 6, 10, 15, 21, 28, 36, 45, 55
2)	<div style="border: 2px solid orange; padding: 10px; display: inline-block; margin-bottom: 10px;"> <p>1 12 81</p> <p> 39 49 45</p> <p> 10 78 4</p> </div> <p>From the box above, identify any triangular numbers.</p>	1, 10, 45, 78
3)	Write down a number less than 100 that is a triangular number and a square number.	1 or 36
4)	Which two-digit triangular number with 6 factors is also a multiple of 7?	28 7×4 Factors: 1, 2, 4, 7, 14, and 28
5)	<p>a) What is the 5th triangular number?</p> <p>b) What is the 6th triangular number?</p> <p>c) Find the sum of the 5th and 6th triangular number.</p> <p>d) What type of number is your answer to part (c)?</p>	<p>a) 15</p> <p>b) 21</p> <p>c) 36</p> <p>d) Square number</p>
6)	<p>At a party, everybody shakes hands with each other, once.</p> <p>Work out how many handshakes there are in total, if there are</p> <p>a) 3 people at the party</p> <p>b) 7 people at the party</p> <p>c) 12 people at the party</p>	<p>a) 3</p> <p>b) 21</p> <p>c) 66</p>

Triangular Numbers - Mark Scheme

	Question	Answer	
	Exam Questions		
1)	The pattern below shows the first 4 triangular numbers 		
(a)	Write down the first four triangular numbers.	(a) 1, 3, 6, 10	(1)
(b)	In the space below, draw pattern 5.	(b) 	(1)
(c)	Write down the 5th triangular number.	(c) 15	(1)
2)	List the first 6 triangular numbers.	Any 3 correct (1) 1, 3, 6, 10, 15, 21 (1)	(2)
3)	Find the difference between the 3rd and 6th triangular numbers.	3rd = 6 and 6th = 21 or 21 - 6 (1) 15 (1)	(2)
4)	The triangular numbers are 1, 3, 6, 10, ... The n th term of this sequence is $\frac{1}{2}n(n + 1)$ Find the 250th triangular number.	$\frac{1}{2} \times 250(250 + 1)$ or 125 \times 251 (1) 31375 (1)	(2)

Triangular Numbers - Mark Scheme

5)	<p>The triangular numbers are 1, 3, 6, 10, ...</p> <p>The nth term of this sequence is</p> $\frac{1}{2}n(n + 1)$ <p>Is 4656 a triangular number?</p>	$\frac{1}{2}n(n + 1) = 4656$ $\frac{1}{2}n^2 + \frac{1}{2}n - 4656 = 0$ <p>or</p> $n^2 + n - 9312 = 0 \text{ (1)}$ $(n - 96)(n + 97) = 0$ <p>or</p> $n = 96 \text{ (1)}$ <p>Yes, 4656 is a triangular number.</p>	(3)
----	---	---	-----

Do you have KS4 students who need additional support in maths?

Our specialist tutors will help them develop the skills they need to succeed at GCSE in weekly one to one online revision lessons. Trusted by secondary schools across the UK.

Visit **thirdspacelearning.com** to find out more.