

### **Prime Factors - Worksheet**

#### Skill

### **Group A - Identifying prime factors**

Identify the prime factors of the following numbers:

**1)** 10

**2)** 12

**3)** 16

**4)** 18

**5)** 30

**6)** 100

**7)** 26

**8)** 42

**9)** 33

**10)** 64

**11)** 105

**12)** 242

### Group B - Writing a number as a product of its prime factors

Express the following as a product of their prime factors. Give your answers in index form:

**1)** 18

**2)** 36

**3)** 90

**4)** 180

**5)** 45

**6)** 135

**7)** 225

**8)** 7

**9)** 28

**10)** 77

**11)** 154

**12)** 616



### **Prime Factors - Worksheet**

#### Group C - Solving problems with prime factors

Use the given facts to solve the prime factor problems below:

- 1) Using the fact that  $2 \times 3 = 6$ , what is 30 as a product of its prime factors?
- 3) Using the fact that  $2 \times 3 = 6$ , what is 120 as a product of its prime factors?
- **5)** Using the fact that  $2^2 \times 3 = 12$ , what is 36 as a product of its prime factors?
- 7) Using the fact that  $2 \times 3 \times 5 = 30$ , what is 15 as a product of its prime factors?
- 9) Using the fact that  $2 \times 3 \times 5 = 30$ , what is 120 as a product of its prime factors?
- **11)** Using the fact that  $2 \times 3^2 \times 5 = 90$ , what is 180 as a product of its prime factors?

- 2) Using the fact that  $2 \times 3 = 6$ , what is 60 as a product of its prime factors?
- **4)** Using the fact that  $2^2 \times 3 = 12$ , what is 60 as a product of its prime factors?
- **6)** Using the fact that  $2^2 \times 3 = 12$ , what is 108 as a product of its prime factors?
- **8)** Using the fact that  $2 \times 3 \times 5 = 30$ , what is 90 as a product of its prime factors?
- **10)** Using the fact that  $2 \times 3^2 \times 5 = 90$ , what is 45 as a product of its prime factors?
- **12)** Using the fact that  $2 \times 3^2 \times 5 = 90$ , what is 360 as a product of its prime factors?

## **Prime Factors - Worksheet**

#### **Applied**

- **1) (a)** Write 860 as a product of prime factors. Express your answer in index form.
  - **(b)** Find the lowest number by which 860 would need to be multiplied to give a square number.
- **2) (a)** Write 2464 as a product of prime factors. Express your answer in index form.
  - **(b)** Find the lowest number by which 2464 would need to be multiplied by to give a cube number.
- 3) If  $A = 3^a \times 5^b$  write the following as a product of prime factors.
  - (a) 3A
  - **(b)** 5*A*
  - **(c)** 25*A*
- **4)** By using their prime factor decomposition, decide whether the following numbers are square, cube or neither.
  - (a)  $2 \times 3$
  - **(b)**  $3^3 \times 7$
  - (c)  $3^2 \times 7^2$
  - (d)  $2^3 \times 5^3$
  - (e)  $2^4 \times 5^4 \times 7^4$
  - **(f)**  $2^6 \times 5^6 \times 7^6$



# **Prime Factors - Exam Questions**

1)	Express 108 as a product of its prime factors.		
		(3 marks)	
2)	Write 36 as a product of its prime factors.		
	Give your answer in index form.		
		(3 marks)	
3)	A number is written as a product of its prime factors as $2^3 \times 3 \times 3$	× 5.	
	Work out the number.		
		(2 marks)	
4)	Given that $p = 2^4 \times 3$		
	(a) Calculate $10p$		
		(2)	
	<b>(b)</b> Write $\frac{p}{4}$ as a product of its prime factors.		
		(1)	
	(c) Write $20p$ as a product of primes.		
		(2) (5 marks)	



## **Prime Factors - Answers**

	Question	Answer
	Skill Questions	
Group A	Identify the prime factors of the following numbers:	
	<b>1)</b> 10	<b>1)</b> 2 and 5
	<b>2)</b> 12	<b>2)</b> 2 and 3
	<b>3)</b> 16	<b>3)</b> 2
	<b>4)</b> 18	<b>4)</b> 2 and 3
	<b>5)</b> 30	<b>5)</b> 2, 3 and 5
	<b>6)</b> 100	<b>6)</b> 2 and 5
	<b>7)</b> 26	<b>7)</b> 2 and 13
	8) 42	<b>8)</b> 2, 3 and 7
	9) 33	<b>9)</b> 3 and 11
	<b>10)</b> 64	<b>10)</b> 2
	<b>11)</b> 105	<b>11)</b> 3, 5 and 7
	<b>12)</b> 242	<b>12)</b> 2 and 11
Group B	Express the following as a product of their prime factors. Give your answers in index form:	
	1) 18	<b>1)</b> $2 \times 3^2$
	<b>2)</b> 36	$ 2) 2^2 \times 3^2$
	<b>3)</b> 90	<b>3)</b> $2 \times 3^2 \times 5$
	<b>4)</b> 180	<b>4)</b> $2^2 \times 3^2 \times 5$
	<b>5)</b> 45	<b>5)</b> $3^2 \times 5$
	<b>6)</b> 135	<b>6)</b> $3^3 \times 5$
	<b>7)</b> 225	<b>7)</b> $3^2 \times 5^2$
	8) 7	<b>8)</b> 7
	9) 28	9) $2^2 \times 7$
	10) 77	<b>10)</b> 7 × 11
	<b>11)</b> 154	<b>11)</b> 2 × 7 × 11
	<b>12)</b> 616	<b>12)</b> $2^3 \times 7 \times 11$



### **Prime Factors - Answers**

#### Group C

Use the given facts to solve the prime factor problems below:

- 1) Using the fact that  $2 \times 3 = 6$ , what is 30 as a product of its prime factors.
- 2) Using the fact that  $2 \times 3 = 6$ , what is 60 as a product of its prime factors.
- 3) Using the fact that  $2 \times 3 = 6$ , what is 120 as a product of its prime factors.
- **4)** Using the fact that  $2^2 \times 3 = 12$ , what is 60 as a product of its prime factors.
- **5)** Using the fact that  $2^2 \times 3 = 12$ , what is 36 as a product of its prime factors.
- **6)** Using the fact that  $2^2 \times 3 = 12$ , what is 108 as a product of its prime factors.
- 7) Using the fact that  $2 \times 3 \times 5 = 30$ , what is 15 as a product of its prime factors.
- 8) Using the fact that  $2 \times 3 \times 5 = 30$ , what is 90 as a product of its prime factors.
- 9) Using the fact that  $2 \times 3 \times 5 = 30$ , what is 120 as a product of its prime factors.
- **10)** Using the fact that  $2 \times 3^2 \times 5 = 90$ , what is 45 as a product of its prime factors.
- **11)** Using the fact that  $2 \times 3^2 \times 5 = 90$ , what is 180 as a product of its prime factors.
- **12)** Using the fact that  $2 \times 3^2 \times 5 = 90$ , what is 360 as a product of its prime factors.

- **1)**  $30 = 6 \times 5$
- $30 = 2 \times 3 \times 5$
- **2)**  $60 = 6 \times 10$
- $60 = 2^2 \times 3 \times 5$
- **3)**  $120 = 6 \times 20$
- $120 = 2^3 \times 3 \times 5$
- **4)**  $60 = 12 \times 5$
- $60 = 2^2 \times 3 \times 5$
- **5)**  $36 = 12 \times 3$
- $36 = 2^2 \times 3^2$
- **6)**  $108 = 12 \times 9$
- $108 = 2^2 \times 3^3$
- **7)**  $15 = 30 \div 2$
- $15 = 3 \times 5$
- **8)**  $90 = 30 \times 3$
- $90 = 2 \times 3^2 \times 5$
- **9)**  $120 = 30 \times 4$
- $120 = 2^3 \times 3 \times 5$
- **10)**  $45 = 90 \div 2$
- $45 = 3^2 \times 5$
- **11)**  $180 = 90 \times 2$
- $180 = 2^2 \times 3^2 \times 5$
- **12)**  $360 = 90 \times 4$
- $360 = 2^3 \times 3^2 \times 5$



# **Prime Factors - Answers**

	Question	Answer
	Applied Questions	
1)	<b>a)</b> Write 860 as a product of prime factors. Express your answer in index form.	<b>a)</b> $2^2 \times 5 \times 43$
	<b>b)</b> Find the lowest number by which 860 would need to be multiplied to give a square number.	<b>b)</b> 5 × 43 = 215
2)	<b>a)</b> Write 2464 as a product of prime factors. Express your answer in index form.	<b>a)</b> $2^5 \times 7 \times 11$
	<b>b)</b> Find the lowest number by which 2464 would need to be multiplied by to give a cube number.	<b>b)</b> $2 \times 7^2 \times 11^2 = 11858$
3)	If $A = 3^a \times 5^b$ write the following as a product of prime factors.	
	<b>a)</b> 3A	<b>a)</b> $3A = 3^{a+1} \times 5^b$
	<b>b)</b> 5A	<b>b)</b> $5A = 3^a \times 5^{b+1}$
	<b>c)</b> 25 <i>A</i>	<b>c)</b> $25A = 3^a \times 5^{b+2}$
4)	By using their prime factor decomposition, decide whether the following numbers are square, cube or neither.	
	<b>a)</b> 2 × 3	a) Neither
	<b>b)</b> $3^3 \times 7$	b) Neither
	<b>c)</b> $3^2 \times 7^2$	c) Square
	<b>d)</b> $2^3 \times 5^3$	d) Cube
	<b>e)</b> $2^4 \times 5^4 \times 7^4$	e) Square
	<b>f)</b> $2^6 \times 5^6 \times 7^6$	f) Square and Cube



# **Prime Factors - Mark Scheme**

	Question	Answer	
	Exam Questions		
1)	Express 108 as a product of its prime factors.	2 × 2 × 3 × 3 × 3 or 2 <sup>2</sup> × 3 <sup>3</sup> 108  2 × 2 × 3 × 3 × 3 or 2 <sup>2</sup> × 3  Any correct factor pair of 108 (1) A fully correct prime factor tree (1) Correct answer (1)	(3)
2)	Write 36 as a product of its prime factors.  Give your answer in index form.	2 36  2 36  2 36  Any correct factor pair of 36 (1) A fully correct prime factor tree (1) Correct answer (1)	(3)



## **Prime Factors - Mark Scheme**

3)		A number is written as a product of its prime factors as $2^3 \times 3 \times 5$ .	8 × 3 × 5 (1) 120 (1)	(2)
		Work out the number.		
4)	(a)	Given that $p = 2^4 \times 3$	(a) $2^4 \times 3 = 48 (1)$ $48 \times 10 = 480 (1)$	(2)
		Calculate 10p.		
	(b)	Write $\frac{p}{4}$ as a product of its prime factors.	<b>(b)</b> $2^2 \times 3$	(1)
	(c)	Write 20 <i>p</i> as a product of primes.	(c) $20 \times 2^4 \times 3$ (1)	(2)
			$2^6 \times 3 \times 5 (1)$	

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