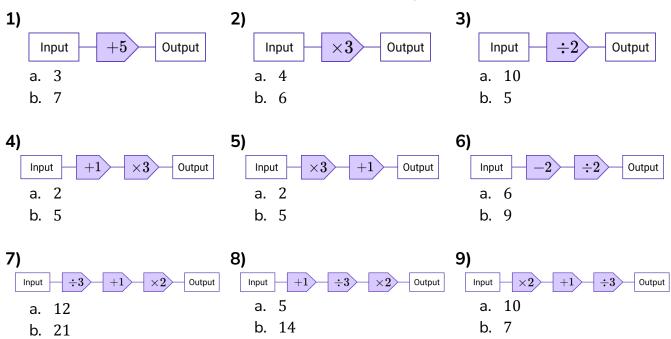


Skill

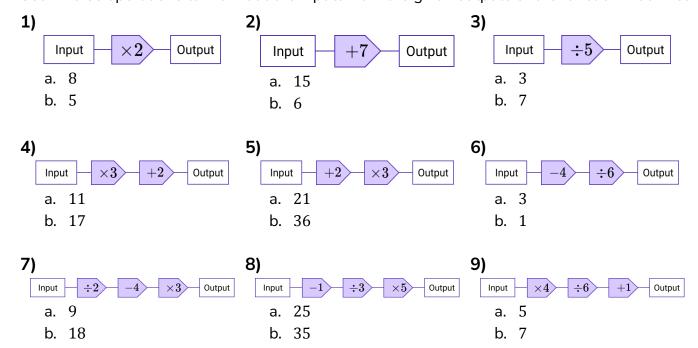
Group A - Finding outputs from function machines

Work out the outputs for the function machines with the given inputs.



Group B - Finding inputs from function machines

Use inverse operations to work out the inputs from the given outputs of the function machines.





Group C - Solving equations using function machines

Draw a function machine to represent the equation and use it to solve the equation.

1)
$$x + 5 = 12$$

2)
$$3x = 15$$

3)
$$\frac{x}{7} = 2$$

4)
$$2x + 1 = 17$$

5)
$$3x - 4 = 14$$

6)
$$2(x + 3) = 24$$

7)
$$\frac{x}{3}$$
 + 1 = 4

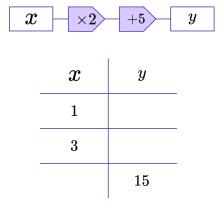
8)
$$\frac{x}{6}$$
 - 3 = 2

9)
$$\frac{x+7}{2} = 6$$

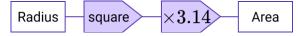


Applied

1) Jen wanted to use a function machine to help her find coordinates on a straight line graph.

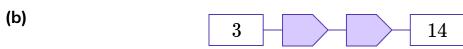


- (a) Complete the table of values.
- **(b)** Is the point (9, 22) on Jen's straight line?
- Neil made a function machine to find the area of a circle? Find the area of a circle with radius 5cm.



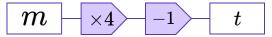
- (b) Use inverse operations to find the radius of a circle with an area of $12.56cm^2$.
- Give two possible function machines that could produce an output of 14 with an input of 3.







4) Function machines can be used to describe and rearrange some formulae. Eg:



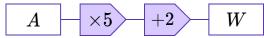
Give the formula t = 4m - 1.

The inverse function machine



Gives the formula $m = \frac{t+1}{4}$.

(a) Write the formula for W, in terms of A, described by the function machine.



(b) Use the inverse function machine to write a formula for A in terms of W.



Function Machines - Exam Questions

1) Here is a function machine:



(a) What is the output when the input is 6?

(1)

(b) What is the input when the output is 26?

(1)

(2 marks)

2) (a) The output of this function machine is 25 when the input is 9. Fill in the missing operation.

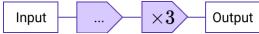
(2)



(2

(b) The output of this function machine is 12 when the input is 5. Fill in the missing operation.

(2)



(4 marks)

3) Fill in the missing values for the function machine.

Input +... Output

(2 marks)

$$3 \longrightarrow 13$$

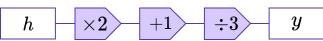
$$5 \longrightarrow 17$$

 $11 \longrightarrow 28$

4) (a) Use the function machine to write a formula for y in terms of h.

.....

(3)



(3)

(b) Use inverse operations to write a formula for *h* in terms of *y*.

(6 marks)



	Question	Answer
	Skill Questions	
Group A	Work out the outputs for the function machines with the given inputs. 1) Input +5 Output a. 3 b. 7 2) Input ×3 Output a. 4 b. 6 3) Input +1 ×3 Output a. 2 b. 5 4) Input +1 Output a. 6 b. 9 7) Input +3 +1 ×2 Output a. 12 b. 21 8) Input +1 +3 ×2 Output a. 5 b. 14 9) Input ×2 +1 +3 Output a. 10 b. 7	1) a. 8 b. 12 2) a. 12 b. 18 3) a. 5 b. 2. 5 4) a. 9 b. 18 5) a. 7 b. 16 6) a. 2 b. 3. 5 7) a. 10 b. 16 8) a. 4 b. 10 9) a. 7 b. 5



Group B

Use inverse operations to work out the inputs from the given outputs of the function machines.

- 1) Input ×2 Output
 - b. 8 b. 5
- 2) Input +7 Output b. 15 b. 6
- 3) Input ÷5 Output b. 3 b. 7
- 4) Input ×3 +2 Output
 b. 11 b. 17
- b. 21 b. 36
- 6) Input -4 ÷6 Output b. 3 b. 1
- 7) Input ÷2 -4 ×3 Output
 b. 9 b. 18
- 8) Input -1 ÷3 ×5 Output
 b. 25 b. 35
- 9) Input ×4 ÷6 +1 Output
 b. 5 b. 7

- **1)** a. 4 b. 2. 5
- **2)** a. 8 b. 1
- **3)** a. 15 b. 35
- **4)** a. 3 b. 5
- **5)** a. 5 b. 10
- **6)** a. 22 b. 10
- **7)** a. 14 b. 20
- **8)** a. 16 b. 22
- **9)** a. 6 b. 9



Group C

Draw a function machine to represent the equation and use it to solve the equation.

1)
$$x + 5 = 12$$

2)
$$3x = 15$$

3)
$$\frac{x}{7} = 2$$

4)
$$2x + 1 = 17$$

5)
$$3x - 4 = 14$$

6)
$$2(x + 3) = 24$$

7)
$$\frac{x}{3}$$
 + 1 = 4

8)
$$\frac{x}{6}$$
 - 3 = 2

9)
$$\frac{x+7}{2} = 6$$

$$\begin{array}{c|cccc} \mathbf{1} & x & +5 & 12 \\ x & = 7 & & & \end{array}$$

$$x \rightarrow x$$

$$x = 5$$

2)

3)
$$x \rightarrow 7$$

$$x = 14$$

$$x = 8$$

$$x = 6$$

6) Input
$$+3$$
 $\times 2$ 24

$$x = 9$$

$$x = 9$$

8) Input
$$\div 4$$
 -3 2

$$x = 30$$

9) Input
$$+7$$
 $\div 2$ 6

$$x = 5$$



	Question	Answer	
	Applied Questions		
1)	Jen wanted to use a function machine to help her find coordinates on a straight line graph. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	(a) $x - x^2 + 5 - y$ $x - y$ $1 - 7$ $3 - 11$ $5 - 15$ (b) No, $9 \times 2 + 5 = 23$ not 22	
	(a) Complete the table of values.(b) Is the point (9, 22) on Jen's straight line?		
2)	(a) Neil made a function machine to find the area of a circle? Find the area of a circle with radius 5cm. Radius square ×3.14 Area	(a) 78.5cm ²	
	(b) Use inverse operations to find the radius of a circle with an area of $12.56cm^2$.	(b) ^{2cm}	
3)	Give two possible function machines that could produce an output of 14 with an input of 3.	(a) E.g. \times 3 + 5, -1 \times 7, \times 4 + 2	
	(a) 3 14	(b) E.g. \times 3 + 5, -1 \times 7, \times 4 + 2	
	(b) 3 14	Different from part a	



4)

Function machines can be used to describe and rearrange some formulae. Eg:

$$m \longrightarrow \times 4 \longrightarrow -1 \longrightarrow t$$

Give the formula t = 4m - 1.

The inverse function machine

$$m$$
 $+1$ t

Gives the formula $m = \frac{t+1}{4}$.

Write the formula for W, in terms of A, described by the function machine.



(b) t

Use the inverse function machine to write a formula for A in terms of W.

(a)
$$W = 5A + 2$$

(b)
$$A = \frac{W-2}{5}$$



Function Machines - Mark Scheme

		Question	Answer	
		Exam Questions		
1)		Here is a function machine:		
	(a)	What is the output when the input is 6?	(a) 40	(1)
	(b)	What is the input when the output is 26?	(b) ⁴	(1)
2)	(a)	The output of this function machine is 25 when the input is 9. Fill in the missing operation.	(a) $9 \times 3 = 27$ Answer of -2	(2)
	(b)	The output of this function machine is 12 when the input is 5. Fill in the missing operation.	(b) $12 \div 3 = 4$ Answer of -1 Input -1 Output	(2)
3)		Fill in the missing values for the function machine. Input $+\dots$ Output $ 3 \longrightarrow 13 $ $ 5 \longrightarrow 17 $ $ 11 \longrightarrow 28$	First box 2 Second box 7	(2)



Function Machines - Mark Scheme

4) (a)	Use the function machine to write a formula for y in terms of h . $\begin{array}{ c c c c c c c c c c c c c c c c c c c$	(a) $ 2h $ $ 2h + 1 $ $ y = \frac{2h+1}{3} $	(3)
(b)	Use inverse operations to write a formula for <i>h</i> in terms of <i>y</i> .	(b) $3y \\ 3y - 1 \\ h = \frac{3y - 1}{2}$	(3)

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