

### Index Notation, Square and Cube Numbers - Worksheet

#### Skill

### Group A - Square and cube numbers

Find the value of:

<b>1)</b> 2 <sup>2</sup>	<b>2)</b> 3 <sup>2</sup>	<b>3)</b> 2 <sup>3</sup>
<b>4)</b> 3 <sup>3</sup>	<b>5)</b> 5 <sup>2</sup>	<b>6)</b> 8 <sup>2</sup>
<b>7)</b> 10 <sup>3</sup>	<b>8)</b> $2^{2} \times 2^{2}$	<b>9)</b> 4 <sup>3</sup>
<b>10)</b> 3 × 2 <sup>3</sup>	<b>11)</b> $3^{2} \times 2^{3}$	<b>12</b> ) $\frac{3^{3}}{3^{2}}$

### Group B - Simplifying expressions involving indices

Simplify fully the expression using index notation:

<b>1)</b> 2 × 2	<b>2)</b> 3 × 3 × 3 × 3	$\textbf{3)} 4 \times 4 \times 4 \times 4 \times 4$
<b>4)</b> $2^{3} \times 2^{5}$	<b>5)</b> $3 \times 3^{3} \times 3^{2} \times 3^{4}$	<b>6)</b> $4^{3} \times 4^{4} \times 4 \times 4^{-2}$
7) $2x^2 \times 4x \times 3x^4$	<b>8)</b> $12x^5 \div 4x^3$	<b>9)</b> $\frac{21x^{-8}}{3x}$
<b>10)</b> $20x^{10} \div 5x^5$	<b>11)</b> $(4x^3)^{-3}$	<b>12)</b> $(8x^3y^4)^{-2}$



### Index Notation, Square and Cube Numbers - Worksheet

#### **Group C - Index Notation**

Simplify fully the expression using index notation:

$1) \ 3x \times 3x \times 3x$	<b>2)</b> $3x^{-1} \times 3x^{-1} \times 3x^{-1}$	$3) \ 3x \ \times \ 3x \ \times \ 3x^{-2}$
4) $\frac{10x^{8}}{20x^{10}}$	<b>5)</b> $\frac{20x^{-8}}{10x^{-10}}$	6) $\frac{100x^{-10}}{200x^{-8}}$
<b>7)</b> $\left(64x^{\frac{1}{2}}\right)^{\frac{1}{2}}$	8) $\frac{3ax^{-6}y^{-4}}{xy}$	<b>9)</b> $2x^{\frac{2}{3}} \times 3x^{\frac{1}{2}}$
<b>10)</b> $x^{\frac{1}{2}} \times x^{\frac{1}{2}}$	<b>11)</b> $x^{\frac{2}{3}} \times x^{\frac{2}{3}}$	<b>12)</b> $(144x^2)^{\frac{1}{2}}$



### Index Notation, Square and Cube Numbers - Worksheet

#### Applied

- 1) (a) The length of a side of a square is 10cm.What is the area of the square?
  - (b) The length of one edge of a cube is 4*cm*. What is the volume of the cube?
- 2) (a) Lyra says "6 squared is 12". Why is Lyra incorrect?
  - (b) Ahmed says "the cube root of 8 is 2".Why is Ahmed incorrect?
- 3) (a) Between which integer values does the square root of 45 lie?
  - (b) Find the value of  $x^{-1} \times x^1$ .
- 4) (a)  $c^a \times c^b = c^{10}$  where *a* and *b* are different positive integers. List the possible values of *a* and *b*.
  - (b) What is 1 to the power of 100?



# Index Notation, Square and Cube Numbers - Exam Questions

2)	(a)	Simplify $4x^2 \times x \times 2x^7$	
			(1) (4 marks)
	(d)	Find the value of $x^0$	
			(1)
	(c)	Find the value of $13^2$	
	(0)	Find the value of $\sqrt{225}$	(1)
	(b)	$\sum_{i=1}^{n} d_i d_i = \sum_{i=1}^{n} d_i d_i = \frac{1}{225}$	(1)
1)	<b>(a)</b>	Find the value of $\sqrt{81}$	

		$+\lambda \wedge \lambda \wedge \lambda \lambda$	(2)
(1	b)	Simplify $\frac{35x^{-12}}{7x^{-5}}$	(2)
(0	c)	Simplify $(3x^3)^3$	
			(2) (6marks)
3) (a	a)	Simplify $\frac{x^{5} \times 20x^{6}}{4x^{8}}$	(2)
()	b)	Simplify	
		$10x^{\frac{1}{4}} \times \frac{1}{2}x^{\frac{1}{5}}$	(2) (4 marks)



## Index Notation, Square and Cube Numbers - Exam Questions

4) (a)  $8 = 2^n$ Find the value of n.

**(b)** 
$$\frac{a^k \times a^{2k}}{\sqrt{a}} = a^n$$

Find the value of n in terms of k.

(4) (5 marks)

(1)

5



# Index Notation, Square and Cube Numbers - Answers

	Question	Answer
Group A	Skill questions	
	Find the value of: 1) $2^{2}$ 2) $3^{2}$ 3) $2^{3}$ 4) $3^{3}$ 5) $5^{2}$ 6) $8^{2}$ 7) $10^{3}$ 8) $2^{2} \times 2^{2}$ 9) $4^{3}$ 10) $3 \times 2^{3}$ 11) $3^{2} \times 2^{3}$ 12) $\frac{3^{3}}{3^{2}}$	<ol> <li>4</li> <li>9</li> <li>8</li> <li>27</li> <li>25</li> <li>6</li> <li>64</li> <li>1000</li> <li>16</li> <li>64</li> <li>64</li> <li>10) 24</li> <li>11) 72</li> <li>3</li> </ol>
Group B	Simplify fully the expression using index notation: 1) 2 × 2 2) 3 × 3 × 3 × 3 3) 4 × 4 × 4 × 4 × 4 4) 2 $^{3}$ × 2 $^{5}$ 5) 3 × 3 $^{3}$ × 3 $^{2}$ × 3 $^{4}$ 6) 4 $^{3}$ × 4 $^{4}$ × 4 × 4 $^{-2}$ 7) 2x <sup>2</sup> × 4x × 3x <sup>4</sup> 8) 12x <sup>5</sup> ÷ 4x $^{3}$	<b>1)</b> $2^{2}$ <b>2)</b> $3^{4}$ <b>3)</b> $4^{5}$ <b>4)</b> $2^{8}$ <b>5)</b> $3^{10}$ <b>6)</b> $4^{6}$ <b>7)</b> $24x^{7}$ <b>8)</b> $3x^{2}$



# Index Notation, Square and Cube Numbers - Answers

	Question	Answer
Group B	9) $\frac{21x^{-8}}{3x}$ 10) $20x^{10} \div 5x^{-5}$ 11) $(4x^{-3})^{-3}$	<b>9)</b> $7x^7$ <b>10)</b> $4x^5$ <b>11)</b> $64x^9$ <b>12)</b> $64x^6y^8$
	<b>12)</b> $(8x^{3}y^{4})^{2}$	
Group C	Simplify fully the expression using index notation:	2
	$1) \ 3x \times 3x \times 3x$	<b>1)</b> $27x^3$
	<b>2)</b> $3x^{-1} \times 3x^{-1} \times 3x^{-1}$ <b>3)</b> $3x \times 3x \times 3x^{-2}$	<b>2)</b> 27x <b>3)</b> 27
	4) $\frac{10x^8}{20x^{10}}$	<b>4)</b> $\frac{1}{2}x^{-2}$
	<b>5)</b> $\frac{20x^{-8}}{10x^{-10}}$	<b>5)</b> $2x^{-2}$
	<b>6)</b> $\frac{100x^{-10}}{200x^{-8}}$	<b>(b)</b> $\frac{1}{2}x$ <b>(7)</b> $4x^{\frac{1}{4}}$
	$\left  7 \right) \left( 64x^{-\frac{1}{2}} \right)^{-\frac{1}{2}}$	<b>8)</b> $3ax^5y^3$
	8) $\frac{3ax^{-6}y^{-4}}{xy}$	<b>9)</b> $6x^{\frac{7}{6}}$
	<b>9)</b> $2x^{\frac{2}{3}} \times 3x^{\frac{1}{2}}$	<b>10)</b> <i>x</i>
	<b>10)</b> $x^{\frac{1}{2}} \times x^{\frac{1}{2}}$	<b>11)</b> $x^{\frac{1}{3}}$
	<b>11)</b> $x^{\frac{2}{3}} \times x^{\frac{2}{3}}$	<b>12)</b> 12 <i>x</i>
	<b>12)</b> $(144x^{2})^{\frac{1}{2}}$	



## Index Notation, Square and Cube Numbers - Answers

	Qı	uestion	An	swer
	Ар	plied Questions		
1)	(a)	The length of a side of a square is 10 <i>cm</i> . What is the area of the square?	(a)	100 <i>cm</i> 2
	(b)	The length of one edge of a cube is 4 <i>cm</i> . What is the volume of the cube?	(b)	64 <i>cm</i> 3
2)	(a)	Lyra says "6 squared is 12". Why is Lyra incorrect?	(a)	6 squared is 36. Lyra did 2 $\times$ 6.
	(b)	Ahmed says "the cube root of — 8 is 2". Why is Ahmed incorrect?	(b)	The cube root is $-2$ . Ahmed has not considered the negative.
3)	(a)	Between which integer values does the square root of 45 lie?	(a)	Between 6 and 7
	(b)	Find the value of $x^{-1} \times x^{1}$ .	(b)	1
4)	(a)	$c^{a} \times c^{b} = c^{10}$ where <i>a</i> and <i>b</i> are different positive integers. List the possible values of <i>a</i> and <i>b</i> .	(a)	9, 1 8, 2 7, 3 6, 4
	(b)	What is 1 to the power of 100?	(b)	1



# Index Notation, Square and Cube Numbers - Mark Scheme

		Question	An	swer	
1)	(a)	Find the value of $\sqrt{81}$	(a)	9	(1)
	(b)	Find the value of $\sqrt{225}$	(b)	15	(1)
	(c)	Find the value of 13 <sup>2</sup>	(c)	169	(1)
	(d)	Find the value of $x^0$	(d)	1	(1)
2)	(a)	Simplify $4x^2 \times x \times 2x^7$	(a)	$8x^{10}$ One mark for correct coefficient One mark for <i>x</i> with correct index number	(2)
	<b>(b)</b>	Simplify $\frac{35x^{-12}}{7x^{-5}}$	(b)	$5x^7$ One mark for correct coefficient One mark for <i>x</i> with correct index number	(2)
	(c)	Simplify $(3x^3)^3$	(c)	$27x^9$ One mark for correct coefficient One mark for <i>x</i> with correct index number	(2)
3)	(a)	Simplify $\frac{x^{5} \times 20x^{6}}{4x^{8}}$	(a)	$5x^3$ One mark for correct coefficient One mark for <i>x</i> with correct index number	(2)
	(b)	Simplify $10x^{\frac{1}{4}} \times \frac{1}{2}x^{\frac{1}{5}}$	(b)	$5x^{\frac{9}{20}}$ One mark for correct coefficient One mark for <i>x</i> with correct index number	(2)



## Index Notation, Square and Cube Numbers - Mark Scheme

		Question	Answer	
4)	(a)	$8 = 2^{n}$ Find the value of <i>n</i> .	(a) 3	(1)
	(b)	$\frac{a \times a^{2k}}{\sqrt{a}} = a^{n}$ Find the value of <i>n</i> in terms of <i>k</i> .	(b) Simplifying numerator correctly to $a^{3k}$ Can been seen anywhere Writing denominator in index for : $a^{\frac{1}{2}}$ Can been seen anywhere	(1) (1)
			Attempt to simplify to a single expression $n = 3k - \frac{1}{2}$	(1)
			Condone $a^{3k-\frac{1}{2}}$ given as final answer Allow indices simplified to a single form e.g $n = \frac{6k-1}{2}$	(1)

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